Math 10/11 Enriched: Section 5.3 Solving Systems of Equations with Radicals

1. Solve for "x". Indicate any extraneous roots and restrictions on the domain:

a)
$$\sqrt{x} = 5$$

b)
$$2\sqrt{x+1} = 5$$

c)
$$\sqrt{3x+1} = 16$$

d)
$$-3\sqrt{4x-1} = -2$$

e)
$$15 + \sqrt{4x - 3} = 9$$

f)
$$\sqrt{2x+25} = \sqrt{x+14}$$

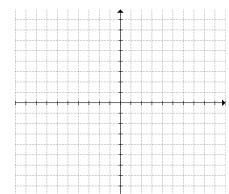
$$g)\sqrt{x} = x + 3$$

h)
$$\sqrt{3x+1} = 2x-6$$

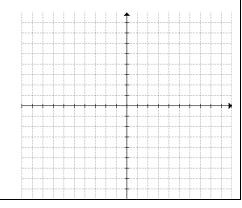
i)
$$3\sqrt{3x+1} = -(x+5)$$

2. Graph the system with the left side as Y1 & right side as Y2. Solve the system by finding all intersection points

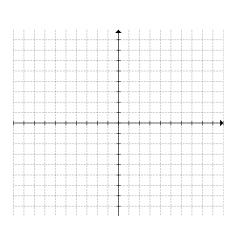
a)
$$\sqrt{x+5} = -x-5$$



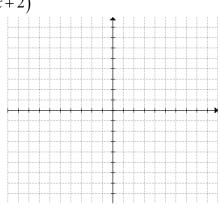
b)
$$\sqrt{3x+1} = x-9$$



c)
$$\sqrt{-x} = \frac{x}{x+2}$$



d)
$$\sqrt{\frac{37}{2} \left(\frac{x}{3} + 1 \right)} = \frac{1}{\left(x + 2 \right)^2}$$



3. Solve each of the following equations. Indicate an extraneous roots:

a)
$$\sqrt{x+2} = \frac{1}{\sqrt{x+2}}$$

b)
$$\sqrt{x^2 - 8} = \sqrt{3x + 2}$$

c)
$$\sqrt{x^2 + 3} = x + 1$$

d)
$$\sqrt{x-2} = 4-x$$

e) $\sqrt{2x+3}$	$-\sqrt{x}$	- 2	=	-
e) $\sqrt{2}x + 3$	$-\sqrt{\chi}$	_	_	4

$$f) \sqrt{x-8} + \sqrt{x} = 2$$

$$g) \sqrt{x} + \sqrt{x-3} = 9$$

h)
$$\sqrt{x-2} + \sqrt{3x-3} = 3$$

i)
$$\sqrt{x+6} = \frac{2}{\sqrt{x+1}} + \sqrt{x+1}$$

$$f) \frac{3}{\sqrt{x}} - 5 = \frac{1 - 2\sqrt{x}}{\sqrt{x}}$$

4. Solve for all real value(s) of "x" $\sqrt{x+10} - \frac{6}{\sqrt{x+10}} = 5$

5. Find all "z" such that $\sqrt{5z+5} - \sqrt{3-3z} - 2\sqrt{z} = 0$

6. It so happens that $\sqrt{1800} + \sqrt{200} = \sqrt{n}$, where "n" is an integer. What is the value of "n"?

7. Find all real values of "x" which satisfy $\sqrt{x^2 + 1} + x^2 + 1 = 90$

8. Find
$$2x + 5$$
 if "x" satisfies $\sqrt{40 - 9x} - 2\sqrt{7 - x} = \sqrt{-x}$

9. Solve for "x"
$$\sqrt{x+\sqrt{x+11}} + \sqrt{x-\sqrt{x+11}} = 4$$

10. Determine the sum of the solution for "x":
$$\sqrt{2x-7} = 2 + \sqrt{x-7}$$

11. Determine the domain of the following function:
$$y = \sqrt{190 - \sqrt{x}}$$

12. For how many real values of "x" is $\sqrt{2211-\sqrt{x}}$ an integer?

13. If $\sqrt{\frac{3}{1} \times \frac{5}{3} \times \frac{7}{5} \times \times \frac{2n+1}{2n-1}} = 9$, then what is the value of "n"? Fermat #21

14. What are all real values of "x" which satisfy:

$$\sqrt{x+2\sqrt{x-1}} + \sqrt{x-2\sqrt{x-1}} = 2\sqrt{x-1}$$
?